

FAST Copper For Broadband Access

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- **R3Q**: Rate (at application level), reach, reliability, quality
- Through fiber/DSL deployment, engineering innovations, and fundamental research
- Four key dimensions: **F**requency, **A**mplitude, **S**pace, **T**ime (FAST)

Why Fiber/Copper?

- Alternatives of broadband access:
 - ▶ **Wireless**: reliability, coverage, and backhaul issues
 - ▶ **Cable modem**: not ubiquitous, bandwidth sharing issues
 - ▶ **Fiber to the closet**: per-customer labor cost prohibitive
 - ▶ **Existing DSL**: **160 million users**, but not fast enough

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 - ▶ **Existing DSL**: **160 million users**, but not fast enough
- **Fiber/Copper**: best of ubiquity, broadband, reliability, and migration
- **Broadband over phone wires**
- Example: AT&T's Lightspeed Project

Where Are Bottlenecks and Where To Improve

- **Attenuation**: Solution from **Space**
- **Crosstalk**: Solutions from **Frequency, Amplitude, Time**

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- Realistic estimates on improvements coming from **research**:
 - ▶ **Frequency**: 2X (even more through signal processing)
 - ▶ **Amplitude**: >2X
 - ▶ **Space**: enabler of rate, reach, reliability
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 - ▶ **Time**: 2X
- Not even bringing in **wider bandwidth, multiple telephone lines, and systems debugging** yet

Key Ideas

- It's not a dedicated line, it's a (multi-carrier) interference channel
 - ▶ From “low frequency” mentality to “high frequency” mentality
 - ▶ Turn competition to cooperation in frequency and time
- It's not a voice line, it's a bursty data and video line
 - ▶ From “deterministic” mentality to “statistical” mentality
 - ▶ Squeeze in more than you have bandwidth for
- A lot of research (and deployment) challenges

Challenges and Connections

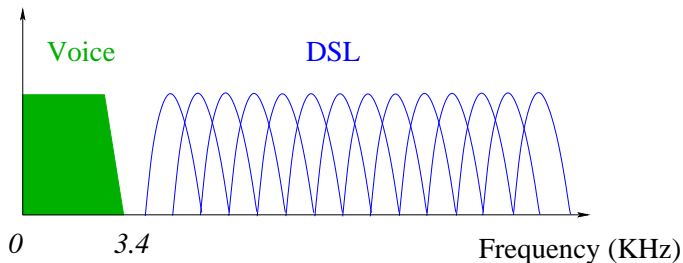
- **Information theory**: multi-carrier interference channel
- **Signal processing**: multi-user transmissions
- **Stochastic theory**: statistical multiplexing
- **Graph theory**: survivable tree design
- **Optimization theory**: nonconvex and globally coupled optimization
- **Networking**: resource allocation and “Layering As Optimization Decomposition”

Our focus today will be **Frequency** and **Time**.

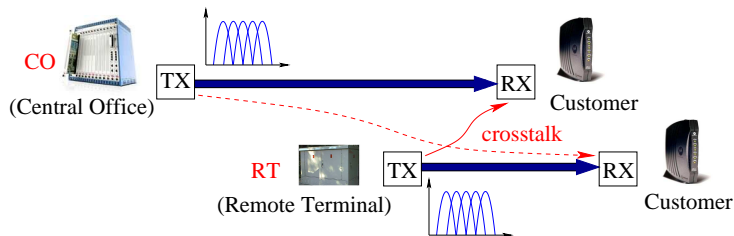
Frequency

Transmission Model

- Copper line can support signal transmissions over a large bandwidth
- Voice transmission: up to 3.4 KHz
- DSL transmissions: up to 30 MHz
 - ▶ Multi-carrier transmissions: Discrete Multitone Modulation



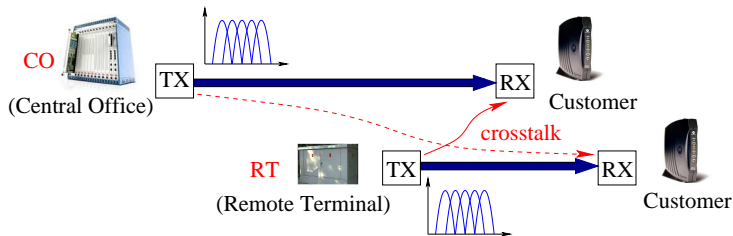
Network and Channel Model



Mathematical model: multi-user **multi-carrier interference** channel

- Each telephone line is a **user** (transmitter-receiver pair)
- Generate mutual **crosstalks** over multiple frequency **tones**

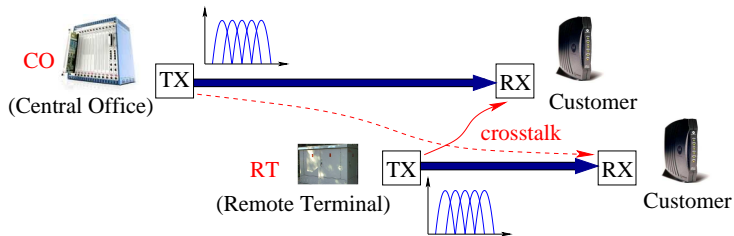
Network and Channel Model



Physical model: mixed CO/RT case

- Channel attenuates with distance
- Central Office (CO) connect customers who are reasonably close
- Remote Terminal (RT) connect customers who are farther away

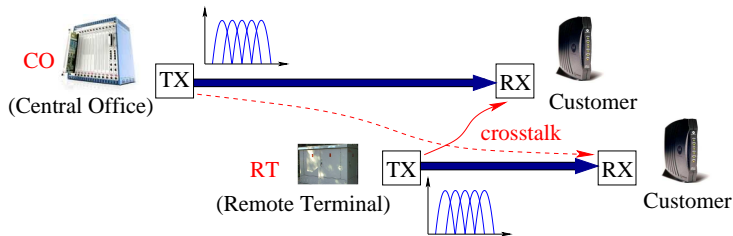
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Frequency-Dependent Channel

- Direct channel gain decreases with frequency
- Crosstalk channel gain increases with frequency

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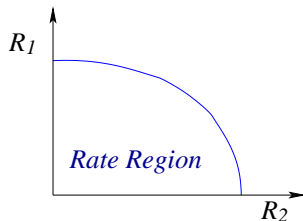


Frequency-Dependent Channel

- Direct channel gain decreases with frequency
- Crosstalk channel gain increases with frequency
- Lead to near-far problem
 - ▶ RT generates **strong** crosstalk to CO line, especially in **high tones**
 - ▶ CO generates **little** crosstalk to RT in all tones

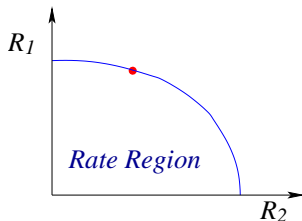
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Rate Region: set of all achievable rate vectors



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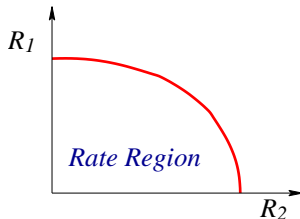
Problem A: (Find One Point On the Rate Region Boundary)

$$\text{maximize}_{\{\mathbf{p}_n \in \mathcal{P}_n\}_n} \sum_n w_n R_n$$

- User n 's achievable rate $R_n = \sum_k \log(1 + \text{SINR}_n^k)$.
 - ▶ No multi-user joint decoding
- User n chooses a power vector $\mathbf{p}_n \in \mathcal{P}_n = \{\sum_k p_n^k \leq P_n^{\max}, p_n^k \geq 0\}$.

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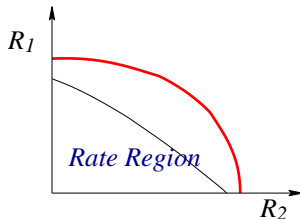
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- Changing different weights trace the **entire rate region boundary**
- A suboptimal algorithm leads to a **reduced** rate region

Properties of Problem A

- **Technical difficulties**

- ▶ **Non-convexity**: total weighted rate not concave in power.
- ▶ **Physically distributed**: local channel information
- ▶ **Performance coupling**: across users (interferences) and tones (power constraint)

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● Difference from the wireless networks

- ▶ **Static** channels
- ▶ **Typical** network topology
- ▶ **Unique** channel frequency responses with good empirical models
- ▶ **Cannot** decode explicit message passing

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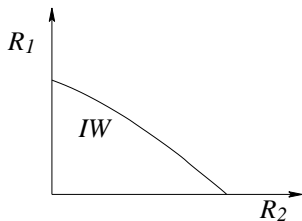
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- **Our Solution**: ASB algorithm

Dynamic Spectrum Management (DSM)

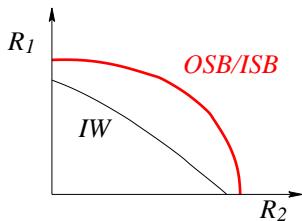
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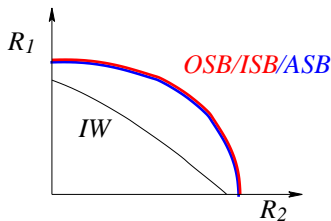
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 - ▶ ASB: Autonomous Spectrum Balancing [Huang et al.'06]

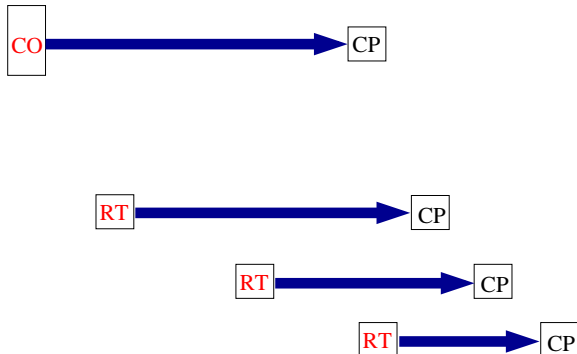


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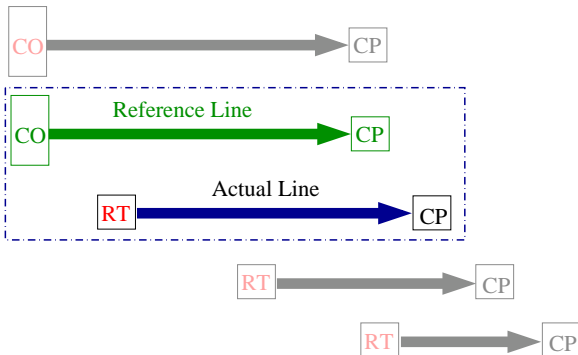
Key Idea: Reference Line

- **Reference line:** static pricing for static channel
 - ▶ A virtual line representative of the typical victim in the network
 - ▶ Good choice: the longest CO line
 - ▶ Parameters (power, noise, crosstalk) are publicly known
- Each user will choose its transmit power to protect the reference line

Reference Line



Reference Line



Reference Line's Rate

- User n's obtains the reference line parameters **locally**

Reference Line
Length & Location



Operator
Database



Reference Power: $p^{k,ref}$

Reference Noise: $\sigma^{k,ref}$

Reference Crosstalk: $\alpha_n^{k,ref}$

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Reference Crosstalk: $\alpha_n^{k,ref}$

- The reference line rate

$$R_n^{ref} = \sum_k \log \left(1 + \frac{p^{k,ref}}{\alpha_n^{k,ref} p_n^k + \sigma^{k,ref}} \right)$$

- ▶ Interference only depends on user n 's transmit power p_n^k
- ▶ Locally computable without explicit message passing

Noncooperative Game

- Users participate in a **non-cooperative game**

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- User n wants to maximize his **payoff**:

$$S_n(\mathbf{p}_n; \mathbf{p}_{-n}) \triangleq R_n^{\text{ref}}(\mathbf{p}_n) + w_n R_n(\mathbf{p}_n; \mathbf{p}_{-n})$$

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- **Best response**: power vector that maximizes his payoff:

$$\mathcal{B}(\mathbf{p}_{-n}) \triangleq \arg \max_{\mathbf{p}_n \in \mathcal{P}_n} S_n(\mathbf{p}_n; \mathbf{p}_{-n})$$

- ▶ Requires solving a **nonconvex** optimization problem
- ▶ **Duality gap** is **zero** (under large number of tones)
- ▶ **Satisfied** in real DSL networks (ADSL: 256 tones, VDSL: 4096 tones)
- ▶ Can be solved using **dual decomposition**

Solution of the Game: Nash Equilibrium

- **Nash Equilibrium (N.E.):** $\mathbf{p}^* = \{\mathbf{p}_n^*, \forall n\}$
- Everyone is happy with the result
- **Fixed point solution** of all users' best responses

$$\mathbf{p}_n^* = \mathcal{B}(\mathbf{p}_{-n}^*), \forall n$$

- Stable outcome of the game

Frequency Selective Water-filling

- Under **high SNR approximation** of the reference line

$$B_n^k(\mathbf{p}_{-n}) = \left(\frac{w_n}{\lambda_n + \alpha_n^{k,\text{ref}} / \sigma^{k,\text{ref}} \cdot \mathbf{1}_{\{p^{k,\text{ref}} > 0\}}} - \sum_{m \neq n} h_{n,m}^k / h_{n,n}^k p_m^k - \sigma_n^k \right)^+$$

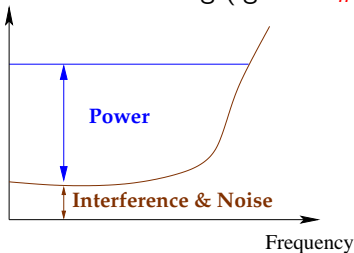
- ▶ Reference line is **not active** in high frequency tones
- Special case: traditional water-filling (ignore $\alpha_n^{k,\text{ref}} / \sigma^{k,\text{ref}}$)

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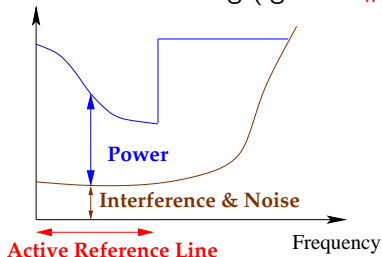
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Frequency-Selective Water-Filling

Convergence of ASB Algorithm

- **ASB** Algorithm: users update their individual power allocation according to **best responses** either sequentially or in parallel

Theorem

ASB algorithm *globally* and *geometrically* converges to the *unique* N.E. if the crosstalk channel is *small*, i.e.,

$$\max_{n,m,k} \frac{h_{n,m}^k}{h_{n,n}^k} < \frac{1}{N-1}.$$

- **Independent** of the reference line parameters.
- Recover the convergence of iterative water-filling as a special case.

Proof: contraction mapping

Proof Outline

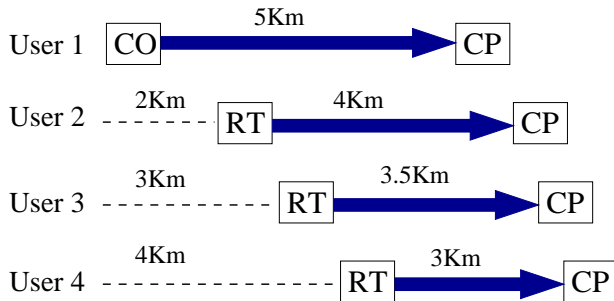
- 1 **Key Lemma**: min-max of an increasing function and an decreasing function is achieved at the intersection.
- 2 **Construct** two such functions based on the ASB algorithm.
- 3 Show the **maximum difference** between the PSD during adjacent iterations is decreasing.

$$\begin{aligned} & \max_n \max \left\{ \sum_k [p_n^{k,t+1} - p_n^{t,t}]^+, \sum_k [p_n^{k,t+1} - p_n^{k,t}]^- \right\} \\ & \leq \max_n \max \left\{ \sum_k [p_n^{k,t} - p_n^{k,t-1}]^+, \sum_k [p_n^{k,t} - p_n^{k,t-1}]^- \right\} \end{aligned}$$

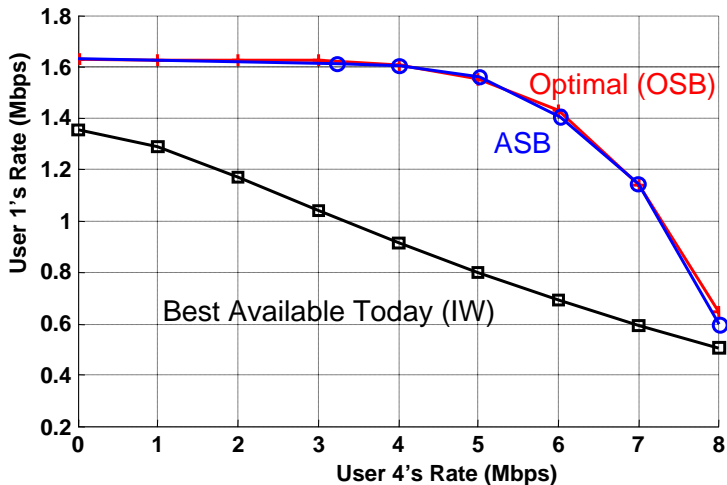
- ▶ Sequential updates: bound the **maximum eigenvalue** of the mapping matrix.
- ▶ Parallel updates: **more realistic** with cleaner proof.

ASB Performance

- **Realistic** industry simulator
- Mixed CO/RT deployment
- Practical channel and background noise models



Achievable Rate Regions of Different Algorithms



Quick Summary

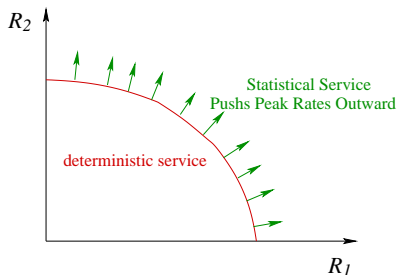
- **Topic:** spectrum management in DSL multiuser interference channels
- **Key idea:** static pricing using reference line
- **Algorithm:** ASB: autonomous, low complexity, and robust
- **Performance:** close to optimal, provable convergence
- **Extension:** asynchronous transmissions with inter-carrier-interferences

Amplitude

Service Provision of Stochastic Traffic

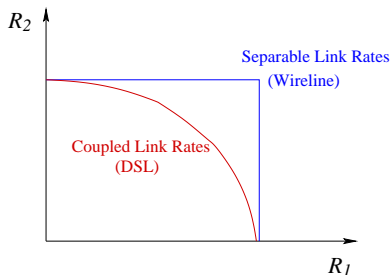
- **Deterministic** service: guarantee **lossless** transmissions.
 - ▶ Peak rate allocation.
- **Statistical** service: meet **probabilistic** QoS requirements.
 - ▶ Example: $\Pr\{\text{Packet Loss}\} < \epsilon$.
 - ▶ More efficient sharing of the same fixed communication channel.
 - ▶ Performance metric: **statistical multiplexing** gain.

Rate Region



- Deterministic service: stay inside the region.
- Statistical service: push outside the region.

Rate Region



- Deterministic service: stay inside the region.
- Statistical service: push outside the region.
- Separable link rates (most wireline): $R_1 \leq C_1, R_2 \leq C_2$
- Coupled link rates (e.g., DSL): $(R_1, R_2) \in \mathcal{C}$

Cross-layer Statistical Multiplexing

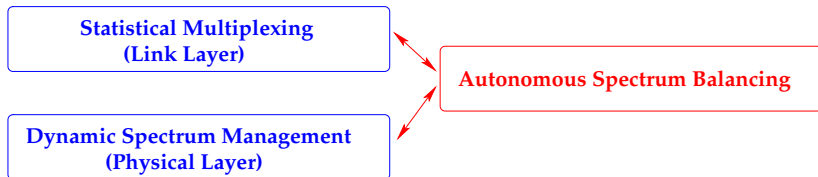
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 - ▶ Only considers **link layer** resource allocation.
 - ▶ Assume underlining link rates are **fixed**.

Cross-layer Statistical Multiplexing

- Previous results on statistical multiplexing in wireline network
 - ▶ Only considers **link layer** resource allocation.
 - ▶ Assume underlining link rates are **fixed**.
- Here we also optimize **physical layer** resource.
 - ▶ Provide **optimal rate allocation** for upper layers.
 - ▶ Additional degree of freedom leads to better performance.

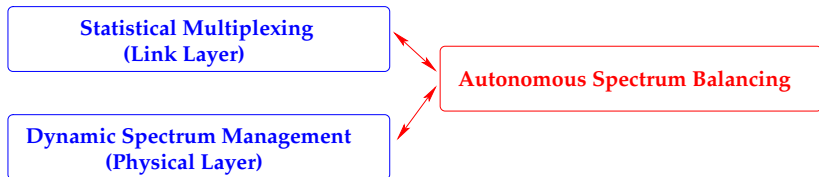
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- Network performance optimization under **stochastic** traffic arrivals.



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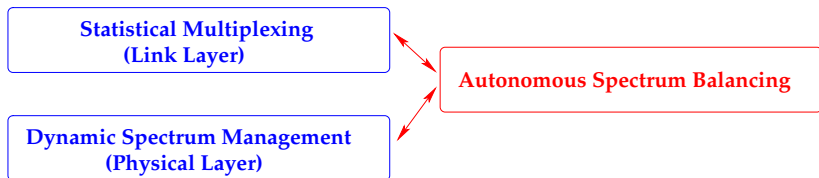
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 - ▶ **Traffic arrival statistics**: mean, peak, variance ...
 - ▶ **QoS requirements**: packet loss, delay, ...

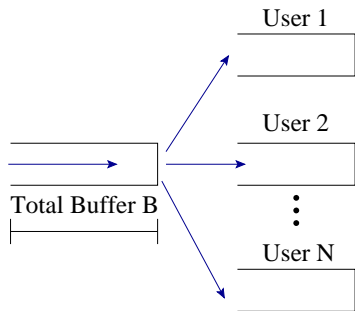
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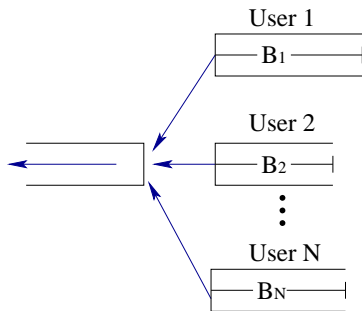


- What we know:
 - ▶ **Traffic arrival statistics**: mean, peak, variance ...
 - ▶ **QoS requirements**: packet loss, delay, ...
- What we want to solve:
 - ▶ Optimal **rate allocation** (physical layer)
 - ▶ Optimal **buffer allocation** (link layer)
 - ▶ Determine the **admission region**

Network Model



Multiplexing Link DSL Users
(a) Downstream Transmissions



Multiplexing Link DSL Users
(b) Upstream Transmissions

Effective Bandwidth

- Simplify the analysis in the asymptotic regime
 - ▶ Large buffer, a lot of users, ...
- Estimate the bandwidth consumption of a **stochastic** traffic by a **constant rate** traffic.
- Depends on
 - ▶ Traffic arrival statistics.
 - ▶ QoS requirements.
 - ▶ Available network resource (e.g., buffer space).
- Many results available:
 - ▶ Large buffer asymptotic (in this talk).
 - ▶ Many source asymptotic (on-going work).

Effective Bandwidth

- Mathematical expression: $g(\delta)$
 - ▶ Function g depends on traffic characteristics
 - ▶ Parameter δ depends on QoS and network resource
 - ▶ mean rate $\leq g(\delta) \leq$ peak rate

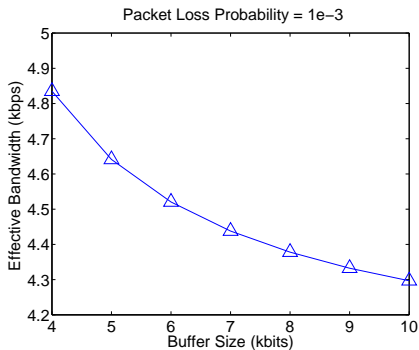
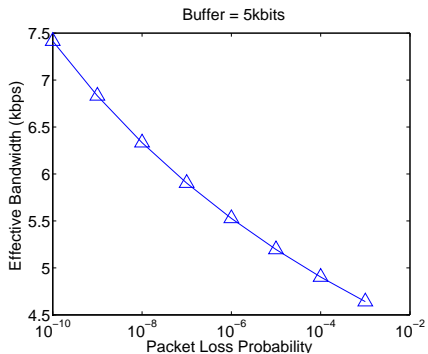
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- Example: Compound Poisson arrival
 - ▶ Arrival rate λ , with exponential file size with mean $1/\mu$
 - ▶ QoS: packet loss prob less than ϵ
 - ▶ Resource: allocated buffer space B
 - ▶ Effective bandwidth:

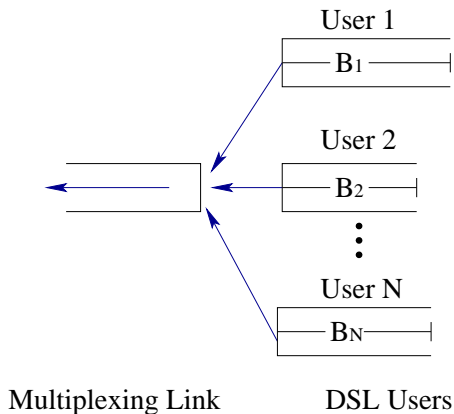
$$g(\delta) = \frac{\lambda}{\mu - \delta} = \frac{\lambda}{\mu - \frac{|\log(\epsilon)|}{B}}$$

Numerical Examples



Average rate 4kbps

Upstream Transmissions



Rate Allocation in Upstream

- Each user has fixed flow traffic characteristics, QoS requirements and buffer space \Rightarrow **fixed** Effective Bandwidth
- Rate allocation problem:

$$\begin{aligned} & \text{maximize} && \sum_i w_i a_i n_i && \text{(total weighted throughput)} \\ & \text{subject to} && \mathbf{c} \in \mathcal{C} && \text{(rate region constraint)} \\ & && n_i g_i \leq c_i, \forall i && \text{(EB less than allocated rate)} \\ & \text{variables} && \mathbf{n}, \mathbf{c} \geq \mathbf{0} && \text{(\# of flows, rate)} \end{aligned}$$

Rate Allocation in Upstream

- Let $c_i = n_i g_i$ and $\bar{w}_i = w_i a_i$
- Rate allocation problem:

$$\text{maximize } \sum_i \bar{w}_i c_i \quad (\text{total weighted rate})$$

$$\text{subject to } \mathbf{c} \in \mathcal{C} \quad (\text{rate region constraint})$$

$$\text{variables } \mathbf{c} \geq \mathbf{0} \quad (\text{rate})$$

- ▶ **Nonconvex** and tightly coupled optimization
- ▶ Can be **efficiently** solved using ASB algorithm.

Rate Allocation in Upstream

- Let $c_i = n_i g_i$ and $\bar{w}_i = w_i a_i$
- Rate allocation problem:

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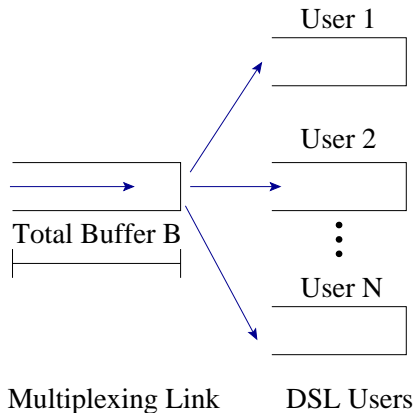
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- Determine accordingly $n_i = c_i / g_i$
 - ▶ Different weights $\{w_i\}$ trace the admission region boundary
- **Implication**: **opportunistic** spectrum management responding to **heterogeneous** traffic characteristics and buffer allocations.

Downstream Transmissions

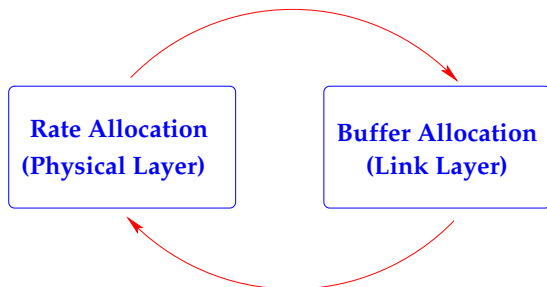


Joint Buffer and Rate Allocation in Downstream

- Joint buffer and rate allocation is **nonconvex**.

Joint Buffer and Rate Allocation in Downstream

- Joint buffer and rate allocation is **nonconvex**.
- Solution: **Alternate Maximization** algorithm
 - ▶ Provable convergence



Buffer Allocation

- Buffer allocation:

$$\text{maximize } \sum_i \bar{w}_i n_i \quad (\text{total weighted throughput})$$

$$\text{subject to } \sum_i B_i \leq B \quad (\text{total buffer constraint})$$

$$n_i g_i \left(-\frac{\log(\epsilon)}{B_i} \right) \leq c_i \quad (\text{EB less than allocated rate})$$

$$\text{variables } \mathbf{n}, \mathbf{B} \geq \mathbf{0} \quad (\# \text{ of flows, buffer})$$

- Can be translated into a quasi-concave optimization, generally requires a **centralized** search.
 - ▶ Closed-form solution possible for special cases.

Algorithm and Convergence

Alternate Maximization Algorithm

Repeat

- ① Solve number of admitted flows (\mathbf{n}) and rate allocation (\mathbf{c}), under **fixed** buffer allocation \mathbf{B} , **using ASB algorithm**.
- ② Solve number of admitted flows (\mathbf{n}) and buffer allocation \mathbf{B} , under **fixed** rate allocation (\mathbf{c}), **using bi-section search (or in closed form in some special cases)**.

Until Convergence

Algorithm and Convergence

Alternate Maximization Algorithm

Repeat

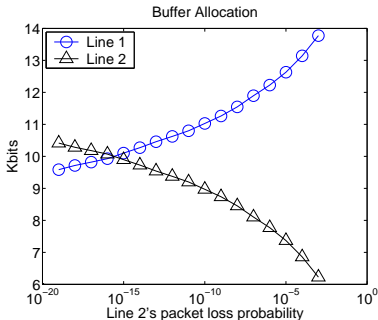
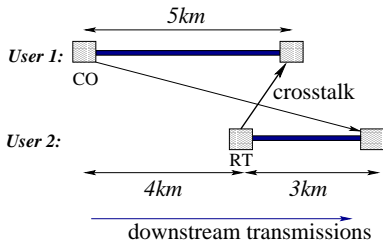
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Until Convergence

Theorem (Convergence of AM Algorithm)

The AM Algorithm converges to a feasible (and typically local optimal) solution of the joint buffer and rate allocation problem.

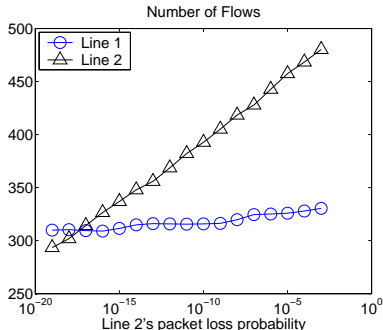
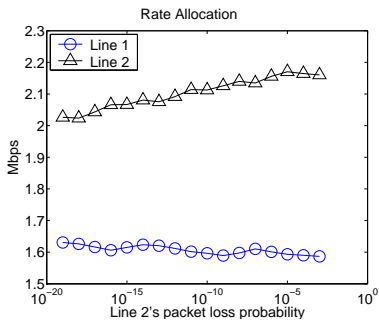
Buffer Allocation



Assumption: Compound Poisson arrivals (both lines), line 1 has fixed QoS requirement

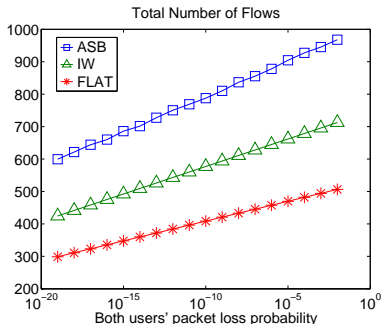
Implication: Relaxed QoS reduces the need for buffer space (line 2).

Rate Allocation and Number of Flows



Implication: Relaxed QoS increases rate allocation and admitted flows.

Different Power Control Algorithms

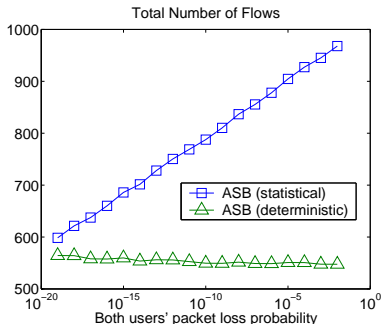


Notations:

- **ASB**: Autonomous Spectrum Sharing (what we proposed)
- **IW**: Iterative Water-filling (best distributed algorithm available today)
- **FLAT**: Flat power allocation (currently used in DSL operations)

Implication: ASB provides the optimal rate region.

Statistical Multiplexing Gain



Implication: large statistical multiplexing gain.

Quick Summary

- **Framework:** cross-layer statistical multiplexing in interference limited DSL networks.
- **Algorithm:** dynamically adjust to traffic characteristics, QoS requirements, network topology, and interference structure.
- **Performance:** substantial performance gain over deterministic service and static spectrum management.
- **Extension:** delay sensitive multimedia traffic.

Summary

Conclusion and Promise

- Presents intellectually challenging **research issues** in broadband access networking
- Motivates many **new problems** in optimization theory, information theory, signal processing, networking, stochastic systems
- Offers an opportunity to make visible, tangible **impacts to practical deployment**

Conclusion and Promise

- Presents intellectually challenging **research issues** in broadband access networking
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- Offers an opportunity to make visible, tangible **impacts to practical deployment**
- The **promise** of FAST Copper:
 - ▶ Rate: **Fast**
 - ▶ Reach: **Ubiquitous**
 - ▶ Reliability: **Survivable**
 - ▶ Quality: **QoS** for triple play

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